



Raman characterization of AB- and ABC-stacked few-layer graphene by interlayer shear modes



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ABSTRACT

Stacking order of layered materials strongly influences their electronic properties. Bernal (AB) and rhombohedral (ABC) stacking are much common in few-layer graphenes. Here, we found that AB- and ABC-stacked few-layer graphenes can be well distinguished by whether their highest-frequency shear modes are observed or not in the Raman spectra at room temperature. This method can be expanded to Raman characterization of the stacking order in other two-dimensional layered materials.

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1. Introduction

Monolayer graphene (1LG) has received intensive interest because of its unique properties [1–5] which provide the impetus for potential applications as electronic and photonic devices. 1LG can be stacked vertically to form N layer graphene (NLG, $N > 2$) with distinctive band structures. For example, 1LG is a zero-gap semi-metal [2,3], whereas bilayer graphene (2LG) is a semiconductor with a tunable band gap [6]. The band structure of trilayer graphene (3LG), in fact, strongly depends on the stacking of the individual graphene sheet. Bernal (AB) and Rhombohedral (ABC) stacking orders are much common in the formation of a few-layer graphene (FLG). AB-stacked 3LG (AB-3LG) has an electrical structure of overlapping linear and quadratic bands [7] while that of ABC-stacked 3LG (ABC-3LG) has a cubic dispersion [8]. When an electric field is applied to 3LG, AB-3LG remains metallic at all fields while ABC-3LG behaves in a similar manner to 2LG with a tunable band gap [9]. The ABC-stacked NLG (ABC-NLG, $N > 3$) is predicted to have even lower kinetic energy than 1LG, 2LG and 3LG, which affords an alternative approach to promote Coulomb interaction between carriers [10]. Besides the band structure, AB-stacked NLG (AB-NLG) and ABC-NLG also exhibit different interlayer screening [11], magnetic state [12,13] and spin–orbit coupling [14]. In view of these differences, researches on NLG require a direct, practical and reliable method to characterize their stacking order at room temperature.

The intrinsic difference in symmetry between AB- and ABC-NLG brings us into the frontier of vibration spectroscopy. Although IR spectroscopy provides a mean of identifying stacking order [15], it requires the specialized instrumentation. Raman spectroscopy, on the other hand, has many advantages over IR spectroscopy and yet has been a versatile tool for studying the properties of graphene [16–18]. For example, the D mode which needs disorders for its activation is widely used to characterize the defects [19] and edges [20–22] in 1LG and FLG. The 2D mode, the second order of the D mode, affords a method to characterize the layer number (N) of AB-NLG ($N = 1 \sim 4$) [23]. Previous Raman characterization of AB- and ABC-stacked FLG was mainly based on the distinctive features of the 2D mode [24–26]. However, the differences in the profile of the 2D mode between AB- and ABC-NLG are much complicated and laser-energy-dependent [24,27,26]. Additionally, the 2D mode is difficult to be applied in N characterization of NLG with $N > 4$, and further to identify stacking order of NLG with $N > 4$. There is still a request for direct and applicable method to characterize the stacking order in NLG.

Interlayer vibrations, including shear (C) and layer breathing (LB) vibrational modes, have received intensive researches in FLG [18,27–33] and transitional metal dichalcogenides [34]. The frequencies of C and LB modes can not be easily observed because of their ultra-low-frequency (ULF) beyond the spectroscopy limitations until Tan et al. successfully detected the highest-frequency C modes in AB-NLG ($N = 2 \sim 16$) [28]. In fact, there are $(N - 1)$ C modes and $(N - 1)$ LB modes for both AB- and ABC-NLG, which we indicate as $C_{N,N-j}$ and $LB_{N,N-j}$, with $j = N - 1, N - 2, \dots, 1$,

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respectively. In this notation [18,33], for a given N , the labels C_{N1} and LB_{N1} are used for the highest frequency C and LB peaks, and the labels $C_{N,N-1}$ and $LB_{N,N-1}$ are used for the lowest frequency C and LB peaks, respectively. The C_{N1} mode is the only C mode thus far observed in AB-stacked FLG at room temperature [28]. The symmetry of AB stacking and weak electron-phonon coupling (EPC) are responsible for the absence of the other C modes in the Raman spectra [28]. Recently, Lui et al. found that the C_{31} mode of ABC-3LG is infrared (IR) active, while the C_{32} mode is Raman (R) active [35]. They observed the C_{32} mode of ABC-3LG at high temperature of about 800 K by laser heating when ABC-3LG was suspended on quartz substrate and the laser power was increased up to ~ 9 mW [35]. The absence of the C_{31} mode of ABC-3LG is because of its Raman inactivity. Therefore, the stacking order can be revealed from the C modes. Now, Si wafer covered with the SiO_2 layer is widely taken as a substrate to support graphene samples on which electronic devices are fabricated. The C mode observation of ABC-3LG by laser heating and sample suspending is not applicable for most samples on SiO_2/Si substrates for the purpose of basic research and device application. Raman activities of the C modes in AB-NLG have been discussed by Tan et al. [28], but those in ABC-NLG are not yet reported.

Here, we measure the ULF Raman spectra of both AB- and ABC-NLG ($N = 3, 4, 5, 6$) deposited on SiO_2/Si substrates at room temperature by a low laser power of 0.5 mW. We find that the C_{N1} modes can only be observed in AB-NLG, but not in ABC-NLG at room temperature. The absence of C_{N1} mode in ABC-NLG with odd N is because of symmetry limitations, while those with even N is probably attributed to small EPC. This can be utilized as a new method to distinguish the AB and ABC stacking in NLG, which will also benefit the stacking order characterization in other layered materials.

2. Experimental

AB- and ABC-NLG are produced by mechanical exfoliation and then transferred onto a Si wafer covered by 93-nm or 300-nm SiO_2 . The layer number of graphene flakes is determined by optical contrast [36,37] and the intensity ratio between the Si peak from SiO_2/Si substrates underneath graphene flakes and that from bare SiO_2/Si substrates [38]. The stacking order is determined by the different lineshape of the 2D mode for AB- and ABC-NLG [26]. Raman measurements are performed by a Jobin-Yvon HR800 Raman system equipped with a liquid nitrogen cooled charge-coupled detector (CCD). The laser excitation wavelength is 633 nm from a He–Ne laser. A typical laser power at samples is less than 0.5 mW to avoid sample heating. The laser plasma lines are removed by using a BraggGrate bandpass filter (OptiGrate Corp.) since these lines would appear in the same spectral range as the C peak. The Rayleigh line is suppressed by using three BraggGrate notch filters (OptiGrate Corp.) with an optical density 3 and a spectral bandwidth $\sim 5\text{--}10$ cm^{-1} . This configuration is similar to that used in Ref. [28]. Argon gas is flowed over the sample to remove the low-frequency Raman modes from air. We use a $\times 100$ objective with a numerical aperture (NA) of 0.90. A 1800 lines per mm grating makes each CCD pixel cover ~ 0.35 cm^{-1} at 633 nm. A spectral resolution ~ 0.6 cm^{-1} is estimated from the full width at half maximum (FWHM) of the Rayleigh peak at 633 nm.

3. Results and discussions

Fig. 1 (a) presents the optical image of a mechanically-exfoliated 3LG flake, whose layer number was confirmed by the measured and calculated optical contrast (Fig. 1(b)). The optical image suggests the 3LG flake is quite uniform. However, the Raman spectra

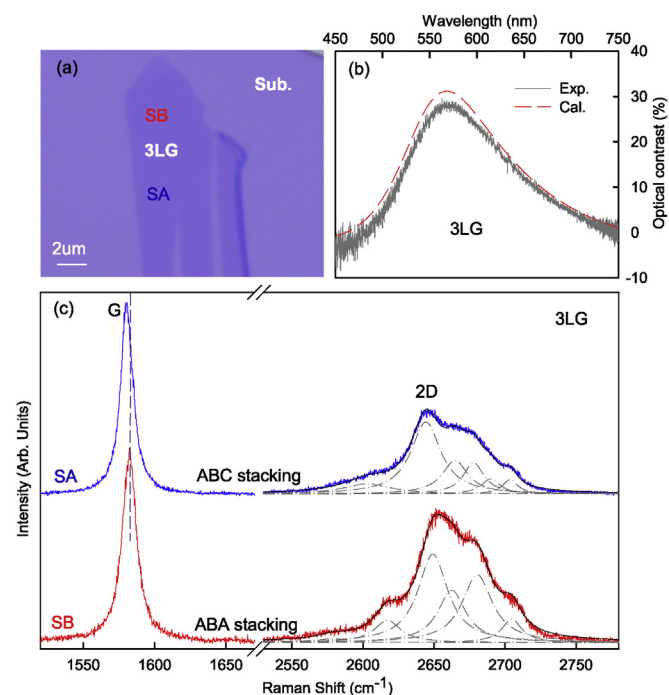


Fig. 1. (a) Optical image of 3LG deposited on the SiO_2/Si substrate. (b) The measured and calculated optical contrast of 3LG. (c) Raman spectra of 3LG measured at two different spots SA and SB, as marked in (a). Dash-dotted lines are the fits to the 2D mode in ABA- and ABC-3LG. (A colour version of this figure can be viewed online).

measured at two spots (SA and SB) in Fig. 1(a) are significantly different. The 2D mode at SB shows an identical spectral profile to a AB-3LG, as shown in Fig. 1(c). The 2D profile in NLG reflects its electronic structure [39]. For example, the 2D mode of 1LG is only one Lorentzian peak because Raman scattering for the 2D mode in the visible range is only one process in triple Raman resonance. However, there are two valence and conduction bands in 2LG, where the incident laser can only couple two pairs of these four bands. The two almost degenerate TO phonons in 2LG can couple all electron bands amongst them, which results in four different sub-peaks for the 2D mode [39]. The number of sub-peaks of 2D mode in NLG will significantly increase with increasing N [23]. For example, there are fifteen sub-peaks in theory for AB-3LG [40]. Actually, using six sub-peaks can reproduce the profile of 2D mode in AB-3LG [23], as depicted by dash-dotted lines in Fig. 1(c) for the 2D mode at SB. AB-3LG at SB can be further verified by the position of the C mode of AB-3LG in Fig. 2, which will be discussed later. Although the optical contrast of the 3LG flake is quite uniform, the 2D mode at SA exhibits a different spectral profile from that at SB, showing a more asymmetric feature, which is identical to that of ABC-3LG [25,26]. Additionally, the G mode of ABC-3LG (~ 1581 cm^{-1}) red-shifts compared with AB-3LG (~ 1582 cm^{-1}), which is attributed to the slight differences between their phonons [25]. The lateral size of the ABC-3LG in Fig. 1(a) around SA is about 4 μm , which can be easily identified from optical images. Mixed ABA and ABC stacking at different area in one graphene flake is very common. Indeed, Lui et al. have found that if the total area associated with the two different stacking orders is considered, $\sim 85\%$ of the area in the samples corresponds to ABA stacking, and $\sim 15\%$ corresponds to ABC stacking [25], which is comparable to that obtained in earlier X-ray diffraction studies of graphite [41].

Similarly, 4-6LG flakes can be firstly identified by optical contrast [36,37] and the Raman mode intensity from Si substrates [38]. Most area of the 4-6LG flakes exhibits the 2D mode of AB-

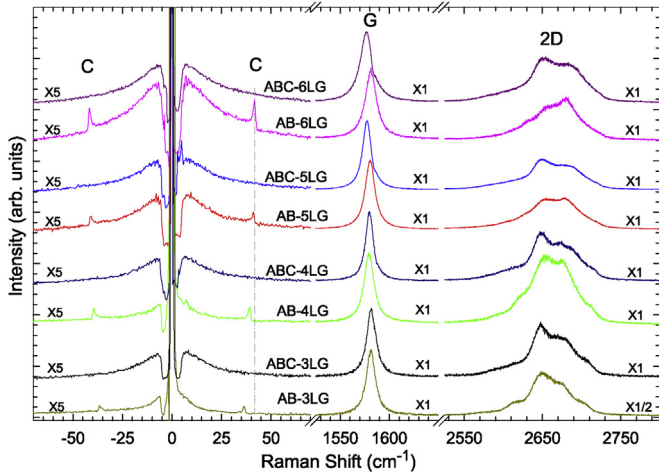


Fig. 2. Raman spectra of AB- and ABC-NLG ($N = 3, 4, 5, 6$) in the C, G and 2D peak spectral regions. The C modes are observed in AB-NLG ($N = 3, 4, 5, 6$), but not in ABC-NLG. (A colour version of this figure can be viewed online).

stacked 4–6LG, while a few area exhibits the 2D mode of ABC-stacked 4–6LG, which is similar to the previous reported results [25,26]. The measured Raman spectra of both AB- and ABC-NLG ($N = 4, 5, 6$) are shown in Fig. 2. Fig. S1 in the Supplementary information shows the fits to the 2D mode of AB-4LG and ABC-4LG. Compared with AB-4LG, the red-shifts of the G mode in ABC-4LG is $\sim 1 \text{ cm}^{-1}$, but this value increases up to $\sim 3 \text{ cm}^{-1}$ in ABC-5LG and $\sim 5 \text{ cm}^{-1}$ in ABC-6LG. The possible reason comes from the N -dependent splitting mediated by the weak interlayer coupling [42].

The main differences between AB- and ABC-NLG in the high-frequency region are the peak position of the G mode and the profile of the 2D mode. However, in the ULF region, we can clearly observe the C modes in AB-NLG ($N = 3, 4, 5, 6$) while those in ABC-NLG totally disappear, as shown in Fig. 2. These observed C modes are actually the C_{N1} modes [28]. C_{31} mode in AB-3LG lies at $\sim 38 \text{ cm}^{-1}$, which is consistent with our previous results [28]. The C_{31} mode increases into $\sim 40 \text{ cm}^{-1}$ (C_{41}) in AB-4LG, $\sim 42 \text{ cm}^{-1}$ (C_{51}) in AB-5LG, $\sim 43 \text{ cm}^{-1}$ (C_{61}) in AB-6LG and finally reaches at $\sim 44 \text{ cm}^{-1}$ in graphite. Besides the observed C_{N1} mode in AB-NLG, other C modes are also expected to appear in Raman spectra [28]. For example, the C_{32} mode ($\sim 22 \text{ cm}^{-1}$) in AB-3LG, the C_{43} ($\sim 17 \text{ cm}^{-1}$) and C_{42} ($\sim 31 \text{ cm}^{-1}$) mode in AB-4LG [28]. However, except the C_{N1} mode, other C modes is too weak to be observed as a result of the symmetry limitation or a small EPC [28]. Thus, one reason for the absence of the C_{N1} mode in ABC-NLG probably comes from the intrinsic difference in symmetry between AB- and ABC-NLG, which makes the C_{N1} mode in ABC-NLG Raman inactive. Another reason is attributed to its small EPC.

The symmetry of the crystal allows us to denote the lattice vibrations, from which we can determine each Raman (R) active vibration. For example, graphite belongs to D_{6h} with its C mode represented by E_{2g}^2 , which is R active. The symmetry of AB-NLG ($N = 2, 3, 4, 5, \dots$) strongly depends on N , which can be divided into D_{3d} for even number of NLG (ENLG) and D_{3h} for odd number of NLG (ONLG). There are $(N-1)$ doubly degenerate C modes in NLG. As shown in Fig. 3(c) there are two and three C modes expected in AB-3LG and AB-4LG, respectively. Because of their difference in symmetry, the denotations of C modes are significantly different. $(N-1)$ C modes in ENLG and ONLG are represented by $\frac{N}{2}E_g + \frac{N-2}{2}E_u$ and $\frac{N-1}{2}E'' + \frac{N-1}{2}E'$, respectively. E_g and E' are R active, E_u is Infrared (IR) active, E'' is both R and IR active. According to their Raman tensors [43], only E_g and E' can be observed under back-scattering configuration. Symmetry, frequency and normal mode displacement for each C mode of AB-3LG and AB-4LG are depicted in Fig. 3. The C_{N1}

mode in AB-stacked ENLG (E_g), ONLG (E') and graphite (E_{2g}^2) are all R active, which has been experimentally observed [28]. Accordingly, ABC-NLG belongs to D_{3d} with their C modes represented by $\frac{N-1}{2}E_g + \frac{N-1}{2}E_u$ for ONLG and $\frac{N}{2}E_g + \frac{N-2}{2}E_u$ for ENLG. Symmetry, frequency and normal mode displacement for each C mode of ABC-3LG and ABC-4LG are also depicted in Fig. 3. It should be noticed that the C_{N1} mode in ABC-stacked ENLG (E_g) is R active, whereas that in ABC-stacked ONLG (E_u) is IR active. It suggests that the absence of the C_{N1} mode in ABC-NLG ($N = 3, 5, 7, \dots$) is the result of their intrinsic difference in symmetry between AB- and ABC-NLG. So we expect that AB- and ABC-NLG ($N = 3, 5, 7, \dots$) can be distinguished by whether their C_{N1} modes are observed or not, as shown in Fig. 2 for 3LG and 5LG. The C_{N1} modes (E_g) in ABC-NLG ($N = 4, 6, 8, \dots$) are R active, thus, these C modes are expected to appear in Raman spectra as that in AB-NLG ($N = 4, 6, 8, \dots$). However, we did not observe any C mode in ABC-4LG and ABC-6LG (Fig. 2). The possible reason comes from its small EPC, which is identical to the absence of other C modes except the C_{N1} modes in AB-NLG [28]. Because the electronic structure of ABC-NLG is different from that of AB-NLG, the different EPC strength for the C_{N1} mode compared with that in AB-NLG is expected. Thus, the EPC strength should be responsible for the absence of the C_{N1} modes in ABC-NLG ($N = 4, 6, 8, \dots$), which needs further calculations. The absence of the C_{N1} modes in ABC-NLG ($N = 3, 4, 5, 6$), with the reason either from symmetry limitations in ONLG or from EPC in ENLG, affords a direct and effective method to characterize the stacking order in NLG.

Next, we analysis the optical activities of $(N-1)$ doubly-degenerated C modes in ABC-NLG ($N \geq 3$) based on their vibration displacements obtained from a simple linear-chain model (LCM). LCM has been applied to obtain the dependencies of the frequencies of C modes (ω_C) on N in both FLG [28] and transition metal dichalcogenides [43], where only the nearest interlayer coupling is considered in layered materials. Each graphene layer in NLG can be considered as a single atom in LCM, where we do not need to account the stacking order. Thus, we can also apply LCM to ABC-NLG. By solving the dynamic matrix, we obtain a general relation between $\omega_C(N)$ and N as follows: $\omega_C(N) = \omega_C(2)\sqrt{1 \pm \cos(N_0\pi/N)}$ ($N \geq 2N_0$, N_0 is an integer: 1, 2, 3, 4, ...), where $\omega_C(2) = (1/\sqrt{2}\pi c)\sqrt{\alpha/\mu}$ is the C mode frequency in 2LG, $\mu = 7.6 \times 10^{-8} \text{ g/cm}^2$ is the mass of one graphene sheet per unit area, c is the speed of light, $\alpha \sim 12.8 \times 10^{18} \text{ N/m}^3$ is the interlayer force constant per unit area. As shown in Fig. 4(a), a pair of branches generate from $(2N_0)$ LG where the mode frequency of one branch (denoted by $C_{2N_0}^+$) increases with increasing N and that of another branch (denoted by $C_{2N_0}^-$) decreases with increasing N . The modes of the $C_{2N_0}^+$ and $C_{2N_0}^-$ branches are actually the C_{N1} and $C_{N,N-1}$ modes, respectively [18,33]. By solving the dynamic matrix, we also obtained the vibration displacements from which we can determine whether each mode is R active (Fig. 2(c)). The rectangle and triangle in Fig. 4 denote the R and IR active modes, respectively. The optical activity of each C mode in AB-NLG has been discussed by Tan et al. [28]. The C_2^+ branch is either R or both R and IR active, while the C_2^- branch is R active. Only the C_2^+ branch is detected in the experiment. The absence of the C_2^- branch was attributed to its small EPC.

Finally, we mainly focused on the C_2^+ and C_2^- branches in ABC-NLG. It should be noted that $\omega_C(2)$ is absent in ABC-NLG because at least three layers are required in ABC stacking order. However, we still denote the pair of branches from 2LG by C_2^+ and C_2^- in ABC-NLG as that in AB-NLG. The C_2^- branch of ABC-NLG is R active, but we do not detect any C modes (Fig. 2). Lui et al. recently observed the C_{32} mode (lying in C_2^- branch) in ABC-3LG suspended on quartz substrate at high temperature of about 800 K by increasing the laser power up to $\sim 9 \text{ mW}$ [35]. The high laser power will remove the

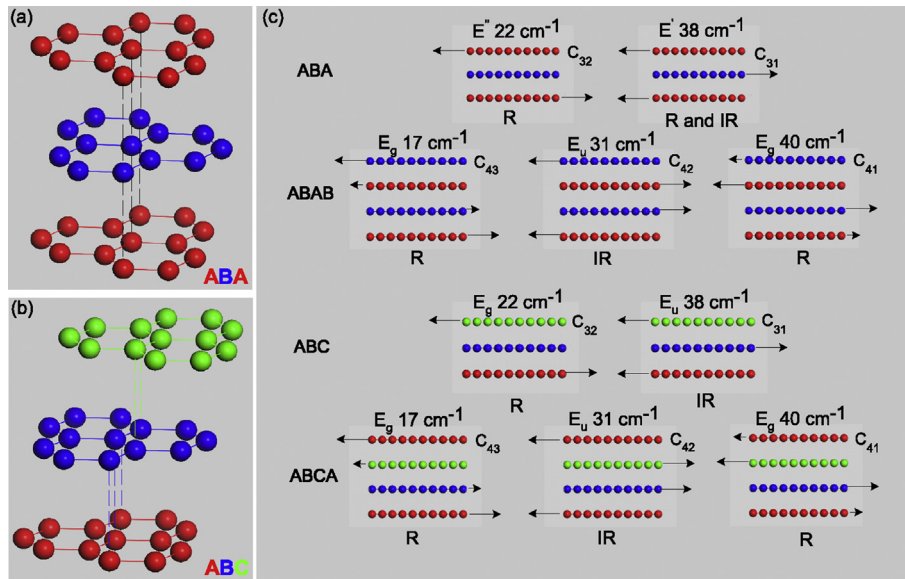


Fig. 3. Schematic illustration of AB-3LG (a) and ABC-3LG (b) in atomic structure. (c) Symmetry, frequency and normal mode displacement for each C mode of AB- and ABC-NLG ($N = 3, 4$). The C_{31} mode of AB-3LG is Raman (R) active while that of ABC-3LG is Raman-inactive. The C_{41} modes of AB- and ABC-4LG are both R active. (A colour version of this figure can be viewed online).

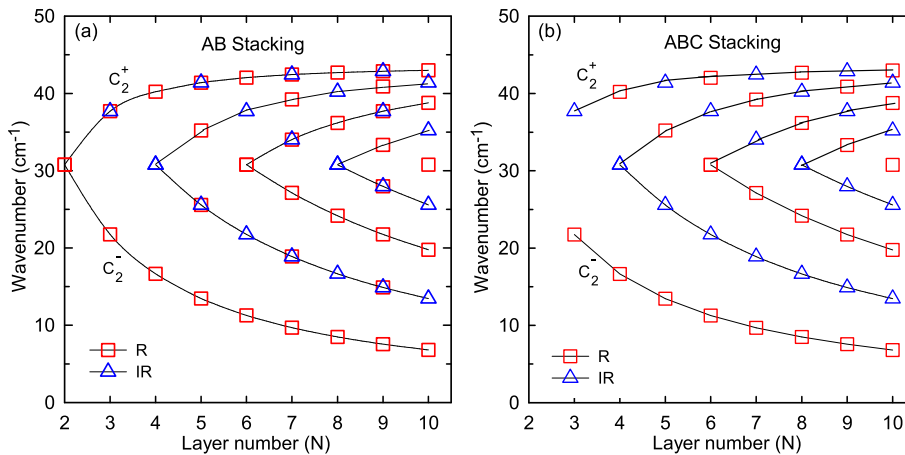


Fig. 4. The frequencies of C modes in NLG for AB stacking (a) and ABC stacking (b) as a function of N . The rectangles and triangles denote the Raman (R) and infrared (IR) active modes, respectively. C_2^+ and C_2^- denote the pair of branches from 2LG. (A colour version of this figure can be viewed online).

surface adsorbates, which also allows the observation of LB modes in AB-NLG [30]. The C_{31} mode in ABC-3LG is absent in their experiments [35] even the laser power was increased up to ~ 9 mW. This is completely consistent with our results in Fig. 2 because the C_{31} mode is R inactive (Fig. 3(c)).

We measured the ULF Raman spectra of AB-3LG, AB-4LG and AB-5LG which are suspended on Si substrates by increasing the laser power to ~ 10 mW, but didn't detect any C mode (Supplementary information, Fig. S2) because of the strong background induced by the intense laser power. The C_{32} intensity in ABC-3LG is predicted to be ~ 0.57 times that of the C_{31} mode in AB-3LG [35], thus, the absence of the C modes in AB-3LG suspended on SiO₂/Si substrates excited by a laser power of ~ 10 mW suggests that we cannot detect any C mode even if the suspended ABC-3LG on SiO₂/Si substrates is excited by a laser power of ~ 10 mW. Recently, Luo et al. predict that the C_{N1} mode in ABC-stacked ENLG has a much smaller intensity than the $C_{N,N-1}$ mode [44]. This is consistent with the absence of the C_{N1} mode in ABC-stacked ENLG, as shown in Fig. 2. Thus, the absence of the C_{N1} mode in ABC-NLG can be utilized

to characterize the stacking order in FLG at room temperature.

4. Conclusion

In conclusion, we observed the highest-frequency C modes (C_{N1}) in AB-NLG ($N = 3, 4, 5, 6$), but not in ABC-NLG. The absence of the C_{N1} mode in ABC-3LG and ABC-5LG results from the symmetry limitations, whereas that in ABC-4LG and ABC-6LG probably comes from the weak electron-phonon coupling. AB- and ABC-NLG can be effectively characterized by whether their C_{N1} modes are observed or not at room temperature. This affords a direct and reliable method to distinguish different stacking order in FLG at room temperature. It also benefits the characterization of stacking order in other two-dimensional layered materials.

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Appendix A. Supplementary data

Supplementary data related to this article can be found at <http://dx.doi.org/10.1016/j.carbon.2015.11.062>.

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